An optical transmission spectrum of the giant planet WASP-36 b

L. Mancini,1,2* J. Kemmer,1 J. Southworth,3 K. Bott,4 P. Mollière,1 S. Ciceri,1 G. Chen5,6 and Th. Henning1

1Max Planck Institute for Astronomy, Königstuhl 17, D-69117 Heidelberg, Germany
2INAF – Osservatorio Astrofisico di Torino, via Osservatorio 20, I-10025 – Pino Torinese, Italy
3Astrophysics Group, Keele University, Keele ST5 5BG, UK
4Exoplanetary Science at UNSW, Australian Centre for Astrobiology, School of Physics, UNSW Australia
5Key Laboratory of Planetary Sciences, Purple Mountain Observatory, Chinese Academy of Sciences, Nanjing 210008, China
6Instituto de Astrofísica de Canarias, Vía Láctea s/n, E-38205 La Laguna, Tenerife, Spain

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ABSTRACT

We measured a decreasing radius from bluer to redder passbands with a confidence level of \( 11 \sigma \). The radius variation is roughly 1 pressure scale heights between the \( g' \) and the \( z' \) bands. This is too strong to be Rayleigh scattering in the planetary atmosphere, and implies the presence of a species which absorbs strongly at bluer wavelengths.

Key words: techniques: photometric – stars: fundamental parameters – stars: individual: WASP-36 – planetary systems.

1 INTRODUCTION

Transiting hot Jupiters are a class of exoplanets which are very suitable for detailed study of their physical and orbital parameters. They are gas-giant planets with short orbital periods (mass \( M_p > 0.3 M_{\text{Jup}} \) and period \( P < 10 \) d), and many of them are now known orbiting bright stars. Their relatively large sizes usually give deep transits (typically 0.5–3.5 per cent) which are well-suited for observation and analysis. Another particular advantage of transiting hot Jupiters is their suitability for transmission spectroscopy, which can yield constraints on the chemical composition at the terminator of their atmospheres from transit depth measurements at multiple wavelengths. Depending on the temperature of the planet’s atmosphere, it is possible to investigate the presence of several molecules (e.g. \( \text{H}_2\text{O}, \text{CO}, \text{CO}_2 \) and \( \text{CH}_4 \)) at infrared (IR) wavelengths. The blue region of the visual wavelength range is also important to study, as it allows constraints to be placed on the presence of Rayleigh scattering or particular atomic absorption features (e.g. Na). There has been significant progress in this field in the last few years, and many exoplanets have been observed using transmission spectroscopy. The resulting transmission spectra show an unexpectedly diversity of the atmospheres of hot Jupiters, in particular the amount of cloud at observable pressure levels (Sing et al. 2016).

Whilst most of these studies were performed at IR wavelengths, a small set of planets have also been studied at optical wavelengths from space with the \textit{Hubble} and the \textit{Spitzer} telescopes (i.e. HD 189733 b: Pont et al. 2013; HD 209458 b: Désert et al. 2008; HAT-P-1 b: Nikolov et al. 2014; HAT-P-12 b: Sing et al. 2016; WASP-6 b: Nikolov et al. 2015; WASP-12 b: Sing et al. 2013; WASP-17 b: Sing et al. 2016; WASP-19 b: Huitson et al. 2013; WASP-31 b: Sing et al. 2015; WASP-39 b: Fischer et al. 2016) and from large ground-based telescopes such as the Very Large Telescope (GJ 1214 b: Bean, Miller-Ricci Kempton & Homeier 2010; Bean et al. 2011; WASP-19 b: Sedaghati et al. 2015), the Gran Telescopio CANARIAS (HAT-P-19 b: Mallonn et al. 2015; WASP-43 b: Murgas et al. 2014), Gemini (HAT-P-32: Gibson et al. 2013a; WASP-12: Stevenson et al. 2014; WASP-29: Gibson et al. 2013b) and Magellan (HAT-P-26: Stevenson et al. 2016; TrES-3: Parviainen et al. 2016; WASP-6: Jordán et al. 2013).

An alternative approach for probing planetary atmospheres is that of transmission photometry, which has a lower spectral resolution but is suitable for ground-based telescopes with smaller apertures and exoplanets orbiting faint stars. Moreover, photometric observations are much less affected by telluric contamination than spectroscopic ones.

In this context, we are carrying out a large programme of transit observations of the known hot Jupiters with an array of medium-sized telescopes in both hemispheres (Mancini & Southworth 2016). In particular, we are using GROND (Gamma-Ray Burst Optical and Near-Infrared Detector), an imaging camera able to obtain light
curves in four optical and three near-IR passbands simultaneously. These are used to improve measurements of the physical properties of the planets and their host stars, and to look for transit-depth variations as a function of wavelength in the optical wavelength region.

In order to have a comprehensive picture, we are investigating both inflated and compact hot Jupiters. Due to their density, the latter should not be optimal targets for transmission-spectrum studies. However, depending on the equilibrium temperature, opacity and chemical composition of their atmospheres, Mie scattering, Rayleigh scattering and molecular opacity could still cause strong variation of the radius of such planets, especially if we compare measurements at the wavelength region 400–500 nm with those at 800–900 nm.

Previous studies with GROND have shown different atmospheric properties: we obtained transmission photometry consistent with flat spectra for several systems (WASP-23 b: Nikolov et al. 2013; WASP-43 b: Chen et al. 2014; WASP-80 b: Mancini et al. 2014a; WASP-67 b: Mancini et al. 2014b), and larger planetary radii at bluer wavelengths for two objects (Qatar-2 b: Mancini et al. 2014c; WASP-103: Southworth et al. 2015). These two latter studies were repeated transit observations produce more precise and robust results. It is interesting to note the large variation that was found in the photometric precision of the near-IR arms is significantly worse than the optical ones (Pierini et al. 2012), so these data will not be used to redetermine the parameters of the planetary system.

The paper is structured as follows. The observations and data reduction are both described in Section 2, while the analysis of the data is presented in Section 3. The refinement of the orbital ephemerides is given in Section 3. In Section 4 we revise the main physical properties of the planetary system. In Section 5 we investigate the variation of the planetary radius as a function of wavelength and, finally, we summarize our results in Section 6.

### 2 OBSERVATION AND DATA REDUCTION

Four transits by WASP-36 b were observed with GROND, which is mounted on the MPG 2.2 m telescope at ESO, La Silla (Table 1). GROND is a seven-channel imaging camera that was built for rapid observations of gamma-ray burst afterglows (Greiner et al. 2008), but is also well-suited for transit observations. GROND can be used to observe simultaneously in four optical passbands (similar to Sloan g’, r’, i’, z’ and three near-IR bands (J, H, K). The optical light is collected by back-illuminated 2048 × 2048 pixel E2V CCDs, with a field of view of 5.4 × 5.4 arcmin² at a scale of 0.158 arcsec/pixel⁻¹. The near-IR channels use 1024 × 1024 pixel Rockwell HAWAI-I arrays, with a field of view of 10 × 10 arcmin² at 0.6 arcsec/pixel⁻¹. The photometric precision of the near-IR arms is significantly worse than the optical ones (Pierini et al. 2012), so these data will not be considered in this work.

Another transit by WASP-36 b was remotely observed in 2014 December through a Cousins R filter with the Zeiss 1.23 m telescope at the Calar Alto Observatory. The telescope is equipped with a 4096 × 4096 pixel DLR-MKIII camera, with a field of view of 21.5 × 21.5 arcmin² at a plate scale of 0.32 arcsec/pixel⁻¹. The CCD was operated without binning, but windowed to shorten the readout time.

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**Table 1.** Details of the transit observations presented in this work. N_{obs} is the number of observations, T_{exp} is the exposure time, T_{obs} is the observational cadence, and ‘Moon illum.’ is the geocentric fractional illumination of the Moon at midnight (UT). The aperture sizes are the radii of the software apertures for the star, inner sky and outer sky, respectively. Scatter is the rms scatter of the data versus a fitted model.

<table>
<thead>
<tr>
<th>Telescope</th>
<th>Date of first obs</th>
<th>Start time (UT)</th>
<th>End time (UT)</th>
<th>N_{obs}</th>
<th>T_{exp} (s)</th>
<th>T_{obs} (s)</th>
<th>Filter</th>
<th>Airmass</th>
<th>Moon illum.</th>
<th>Aperture radii (px)</th>
<th>Scatter (mmag)</th>
</tr>
</thead>
<tbody>
<tr>
<td>MPG 2.2 m</td>
<td>2012 04 15</td>
<td>01:44</td>
<td>04:36</td>
<td>82</td>
<td>90</td>
<td>156</td>
<td>Sloan g'</td>
<td>1.12 → 2.70</td>
<td>23 per cent</td>
<td>30,53,90</td>
<td>0.54</td>
</tr>
<tr>
<td>MPG 2.2 m</td>
<td>2012 04 15</td>
<td>01:44</td>
<td>04:36</td>
<td>82</td>
<td>90</td>
<td>156</td>
<td>Sloan r'</td>
<td>1.12 → 2.70</td>
<td>23 per cent</td>
<td>32,68,85</td>
<td>0.69</td>
</tr>
<tr>
<td>MPG 2.2 m</td>
<td>2012 04 15</td>
<td>01:44</td>
<td>04:36</td>
<td>82</td>
<td>90</td>
<td>156</td>
<td>Sloan i'</td>
<td>1.12 → 2.70</td>
<td>23 per cent</td>
<td>25,55,80</td>
<td>0.76</td>
</tr>
<tr>
<td>MPG 2.2 m</td>
<td>2013 12 30</td>
<td>03:42</td>
<td>08:57</td>
<td>121</td>
<td>100</td>
<td>142</td>
<td>Sloan g'</td>
<td>1.85 → 1.07 → 1.23</td>
<td>2 per cent</td>
<td>27,65,90</td>
<td>0.69</td>
</tr>
<tr>
<td>MPG 2.2 m</td>
<td>2013 12 30</td>
<td>03:42</td>
<td>08:57</td>
<td>122</td>
<td>100</td>
<td>142</td>
<td>Sloan r'</td>
<td>1.85 → 1.07 → 1.23</td>
<td>2 per cent</td>
<td>27,65,90</td>
<td>0.64</td>
</tr>
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<td>MPG 2.2 m</td>
<td>2013 12 30</td>
<td>03:42</td>
<td>08:57</td>
<td>124</td>
<td>100</td>
<td>142</td>
<td>Sloan i'</td>
<td>1.85 → 1.07 → 1.23</td>
<td>2 per cent</td>
<td>19,61,90</td>
<td>0.88</td>
</tr>
<tr>
<td>MPG 2.2 m</td>
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<td>03:42</td>
<td>08:57</td>
<td>121</td>
<td>100</td>
<td>142</td>
<td>Sloan z'</td>
<td>1.85 → 1.07 → 1.23</td>
<td>2 per cent</td>
<td>32,63,91</td>
<td>0.87</td>
</tr>
<tr>
<td>CA 1.23 m</td>
<td>2014 12 11</td>
<td>01:44</td>
<td>06:02</td>
<td>154</td>
<td>90</td>
<td>100</td>
<td>Cousins R</td>
<td>1.66 → 1.42 → 1.79</td>
<td>80 per cent</td>
<td>23,33,60</td>
<td>1.21</td>
</tr>
<tr>
<td>MPG 2.2 m</td>
<td>2015 01 20</td>
<td>01:37</td>
<td>06:16</td>
<td>88</td>
<td>110</td>
<td>156</td>
<td>Sloan g'</td>
<td>2.04 → 1.07 → 1.08</td>
<td>0 per cent</td>
<td>26,66,100</td>
<td>0.83</td>
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<tr>
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<td>2015 01 20</td>
<td>01:37</td>
<td>06:16</td>
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<td>110</td>
<td>156</td>
<td>Sloan r'</td>
<td>2.04 → 1.07 → 1.08</td>
<td>0 per cent</td>
<td>24,62,100</td>
<td>0.61</td>
</tr>
<tr>
<td>MPG 2.2 m</td>
<td>2015 01 20</td>
<td>01:37</td>
<td>06:16</td>
<td>87</td>
<td>110</td>
<td>156</td>
<td>Sloan i'</td>
<td>2.04 → 1.07 → 1.08</td>
<td>0 per cent</td>
<td>24,60,95</td>
<td>0.95</td>
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<tr>
<td>MPG 2.2 m</td>
<td>2015 01 23</td>
<td>02:43</td>
<td>07:16</td>
<td>105</td>
<td>110</td>
<td>156</td>
<td>Sloan g'</td>
<td>1.39 → 1.07 → 1.19</td>
<td>10 per cent</td>
<td>34,94,110</td>
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<tr>
<td>MPG 2.2 m</td>
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<td>02:43</td>
<td>07:16</td>
<td>101</td>
<td>110</td>
<td>156</td>
<td>Sloan r'</td>
<td>1.39 → 1.07 → 1.19</td>
<td>10 per cent</td>
<td>29,55,97</td>
<td>0.43</td>
</tr>
<tr>
<td>MPG 2.2 m</td>
<td>2015 01 23</td>
<td>02:43</td>
<td>07:16</td>
<td>104</td>
<td>110</td>
<td>156</td>
<td>Sloan i'</td>
<td>1.39 → 1.07 → 1.19</td>
<td>10 per cent</td>
<td>30,53,88</td>
<td>0.76</td>
</tr>
<tr>
<td>MPG 2.2 m</td>
<td>2015 01 23</td>
<td>02:43</td>
<td>07:16</td>
<td>103</td>
<td>110</td>
<td>156</td>
<td>Sloan z'</td>
<td>1.39 → 1.07 → 1.19</td>
<td>10 per cent</td>
<td>31,59,107</td>
<td>0.75</td>
</tr>
</tbody>
</table>

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Note: All observations were collected by back-illuminated 2048 × 2048 pixel E2V CCDs, with a field of view of 5.4 × 5.4 arcmin² at a scale of 0.158 arcsec/pixel⁻¹. The near-IR channels use 1024 × 1024 pixel Rockwell HAWAI-I arrays, with a field of view of 10 × 10 arcmin² at 0.6 arcsec/pixel⁻¹. The photometric precision of the near-IR arms is significantly worse than the optical ones (Pierini et al. 2012), so these data will not be considered in this work.
During all the observations the two telescopes were autoguided and defocused in order to improve the photometric precision of the data.

The reduction of the data was performed using the DEPOT pipeline, written in IDL.\(^1\) (Southworth et al. 2014). Briefly, the scientific images were calibrated using master bias and flat-field frames, produced by median-combining individual calibration images. The target and a suitable set of non-variable comparison stars were identified in a reference image, which was used to measure pointing variations by a cross-correlation process. Three apertures were placed by hand around the selected stars and the aperture radii were chosen to obtain the lowest scatter versus a fitted model. Differential photometry was obtained using the APER routine\(^2\) and rectified to zero magnitude by fitting a straight line to the out-of-transit data. The data will be made available at the CDS.\(^3\)

The Calar Alto light curve is plotted in Fig. 1 together with the best one reported in the discovery paper (Smith et al. 2012) for comparison. The GROND light curves are plotted according to date in Fig. 2 and to filter in Fig. 3. A clear anomaly is visible in the GROND data observed on 2015 January 19 (third panel in Fig. 2). This variation is not correlated with the position of the stars on the CCDs, the CCD temperatures, the weather conditions, or vignetting from the dome slit. There is also no obvious astrophysical explanation. We therefore assumed that the anomaly was caused by an unknown instrumental effect and removed the affected data from our analysis.

3 LIGHT CURVE ANALYSIS

We have modelled our new light curves and the best one from Smith et al. (2012), which was observed with the Euler 1.2 m telescope, using the JKTEBOP\(^4\) code (Southworth 2013). Each light curve was fitted using the following parameters: the sum and ratio of the fractional radii\(^5\) \((r_A + r_b\) and \(k = r_b/r_A\)), the orbital period and inclination \((P\) and \(i\)), the time of transit midpoint \((T_0)\) and the linear coefficient of the quadratic limb darkening law \((u_A)\). The second limb darkening coefficient \((u_A)\) was fixed to a theoretical value (Claret 2004). We assumed that the orbit of WASP-36 b is circular (Smith et al. 2012; Zhou et al. 2015).

The APER algorithm, used in our reduction pipeline, usually underestimates the uncertainties in the differential magnitudes. Red noise also affects time series photometry as it is not accounted for by standard error estimation algorithms (e.g. Carter & Winn 2009). We therefore rescaled the error bars to give a reduced \(\chi^2\) of \(\chi^2 = 1\) (e.g. Mancini et al. 2014a; Southworth et al. 2015). Moreover, using the likelihood function defined as in equation (32) of Carter & Winn 2009.

\(^1\) The acronym IDL stands for Interactive Data Language and is a trademark of ITT Visual Information Solutions.

\(^2\) APER is part of the ASTROLIB subroutine library distributed by NASA.

\(^3\) http://cdsweb.u-strasbg.fr/

\(^4\) JKTEBOP is written in FORTRAN77 and is available at: http://www.astro.keele.ac.uk/jkt/codes/jktebop.html

\(^5\) The fractional radii are defined as \(r_A = R_A/a\) and \(r_b = R_b/a\), where \(R_A\) and \(R_b\) are the true radii of the star and planet, and \(a\) is the semi-major axis.
(2009), we performed a wavelet-basis red-noise MCMC analysis for estimating the Gaussian white noise and the correlated red noise for each light curve. They are reported in the last two columns of Table 2. Fig. 4 shows the root mean square of the binned residuals versus the bin size, which is another way to illustrate the photometric precision that we achieved.

3.1 Orbital period determination

We estimated the times of mid-transit by fitting each light curve with JKTEBOP. The uncertainties were obtained using Monte Carlo simulations. We also considered the timing measured by Smith et al. (2012) and Maciejewski et al. (2016). All transit timings (see Table 2) were then fitted with a straight line to obtain the following orbital ephemeris:

\[ T_0 = \text{BJD(TDB)} 245 5569.83771(46) + 1.53736596(24) E, \]

where \( E \) denotes the number of orbital cycles after the reference epoch, and the quantities in brackets denote the uncertainty in the final digit of the preceding number. The residuals of the fit are plotted in Fig. 5. The linear ephemeris is not a good match to the observations – the fit has \( \chi^2 = 3.76 \) – so the uncertainties have been increased to account for this. As our timings comprise only 10 epochs over more than 1000 orbits, and in line with previous work (e.g. Southworth et al. 2014; Ciceri et al. 2015; Mancini et al. 2015), we do not interpret this as an indication of transit time variations.

3.2 Photometric parameters

The best fits to the light curves are shown in Figs 1 and 6. The parameters of the fits are reported in Table 3. The uncertainties of the parameters were estimated for each solution from 10 000 Monte Carlo simulations and through a residual-permutation algorithm.

\[ \text{Table 2. Times of transit mid-point of WASP-36 and their residuals.} \]

<table>
<thead>
<tr>
<th>Time of minimum</th>
<th>Cycle</th>
<th>O-C (JD)</th>
</tr>
</thead>
<tbody>
<tr>
<td>5556.002 21 ± 0.000 55</td>
<td>-9</td>
<td>0.00075091</td>
</tr>
<tr>
<td>5563.687 81 ± 0.000 17</td>
<td>-4</td>
<td>0.00047861</td>
</tr>
<tr>
<td>5577.524 13 ± 0.000 25</td>
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<td>0.00045174</td>
</tr>
<tr>
<td>5583.673 36 ± 0.000 21</td>
<td>9</td>
<td>0.00068535</td>
</tr>
<tr>
<td>6003.374 65 ± 0.000 43</td>
<td>282</td>
<td>0.00013033</td>
</tr>
<tr>
<td>6032.584 90 ± 0.000 28</td>
<td>301</td>
<td>0.00001463</td>
</tr>
<tr>
<td>6032.585 15 ± 0.000 31</td>
<td>301</td>
<td>0.00025994</td>
</tr>
<tr>
<td>6032.585 45 ± 0.000 25</td>
<td>301</td>
<td>0.00055714</td>
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<tr>
<td>6032.585 51 ± 0.000 31</td>
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<tr>
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</tr>
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<td>7045.708 78 ± 0.000 35</td>
<td>960</td>
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</tr>
<tr>
<td>7045.709 15 ± 0.000 18</td>
<td>960</td>
<td>0.00013033</td>
</tr>
</tbody>
</table>

\[ \text{Table 3. Fig. 4 shows the root mean square of the binned residuals for each light curve. They are reported in the last two columns of Table 2. Fig. 4 shows the root mean square of the binned residuals versus the number of points per bin for each of the four transits of WASP-36 observed with GROND and for each filter: green line is } r', \text{ yellow line is } i', \text{ red line is } r \text{ and brown line is } z'. \text{ The dashed lines are proportional to } N^{-1/2} \text{ and are normalized to match the value for bin size } N = 1 \text{ for each light curve.} \]

\[ \text{Normalised Flux} \]

\begin{align*}
\text{Normalised Flux} & \quad 0.975 & \quad 0.980 & \quad 0.985 & \quad 0.990 & \quad 0.995 & \quad 1.000 & \quad 1.005 \\
\text{Normalised Flux} & \quad 0.975 & \quad 0.980 & \quad 0.985 & \quad 0.990 & \quad 0.995 & \quad 1.000 & \quad 1.005 \\
\text{Normalised Flux} & \quad 0.975 & \quad 0.980 & \quad 0.985 & \quad 0.990 & \quad 0.995 & \quad 1.000 & \quad 1.005 \\
\text{Normalised Flux} & \quad 0.975 & \quad 0.980 & \quad 0.985 & \quad 0.990 & \quad 0.995 & \quad 1.000 & \quad 1.005 \\
\end{align*}
The giant planet WASP-36 b

Figure 5. Residuals of the times of mid-transit versus a linear ephemeris. The timings from Smith et al. (2012) are plotted using open circles, from Maciejewski et al. (2016) with a triangle, from GROND with filled circles, and from Calar Alto with an open box.

Figure 6. Phased light curves of WASP-36 from GROND compared to the JKTEBOP best fits. The passbands and central wavelengths are labelled.

The larger of the two error bars was adopted in each case. The final photometric parameters were calculated as the weighted mean of the results in Table 3. We also show the values obtained by Smith et al. (2012) and Maciejewski et al. (2016) for comparison.

4 PHYSICAL PROPERTIES

We have determined the physical properties of the system using the Homogeneous Studies approach (Southworth 2012). The input quantities to this analysis were the photometric parameters (Section 3.2) and the spectroscopic properties of the host star taken from Smith et al. (2012) (effective temperature $T_{\text{eff}} = 5959 \pm 134$ K, metallicity $[\text{Fe/H}] = -0.26 \pm 0.10$ and velocity amplitude $K_A = 391.5 \pm 8.3$ m s$^{-1}$). These were augmented by an estimate of the velocity amplitude of the planet, $K_b$, and the physical properties of the system calculated.

$K_b$ was iteratively adjusted to maximize the agreement between the measured $R_A/a$ and $T_{\text{eff}}$ and those predicted by a set of theoretical models, considering a wide range of possible ages for the host star. Five sets of theoretical models were used (Claret: Claret 2004; Y2: Demarque et al. 2004; BaSTI: Pietrinferni et al. 2004; VRSS: VandenBerg, Bergbusch & Dowler 2006; DSEP: Dotter et al. 2008), yielding five different estimates of each output quantity. We took the unweighted mean of these as the final values, and assigned a systematic error based on the level of agreement among the values obtained using different theoretical models. Statistical errors were propagated through the analysis from the input parameters. The final values are given in Table 4. Our results are in good agreement with those found by Smith et al. (2012) and Maciejewski et al. (2016), but are more precise and robust.

5 VARIATION OF THE PLANETARY RADIUS WITH WAVELENGTH

Being strongly irradiated by their parent stars, the spectra of hot Jupiters are expected to show characteristic absorption features at optical wavelengths. Some of the predicted features include sodium ($\sim 590$ nm), potassium ($\sim 770$ nm), water vapour ($\sim 950$ nm), and Rayleigh scattering at bluer wavelengths. However, the variety of hot-Jupiter transmission spectra suggests a great deal of variation in chemistry and atmospheric dynamics. While Fortney et al. (2005) suggested that a physical dichotomy exists between, essentially, insulated and non-insulated and well-mixed atmospheres (based primarily upon the level of irradiation received by the planet) the species of clouds driving the insulation has been disputed (e.g. Fortney et al. 2008; Zahnle et al. 2009; Knutson, Howard & Isaacson 2010).

The ability of GROND to observe simultaneously in four optical bands makes it a useful tool to detect absorption features and thus probe the atmospheric composition of the planet, by measuring the ratio of the radii in different bands and comparing these values with synthetic spectra. Following the approach of Southworth et al. (2015), we calculated the ratio of the radii in each passband with the other photometric parameters fixed to the best-fitting values. This yielded a set of $k$ values which are directly comparable and whose error bars exclude common sources of uncertainty. The error
which have a stronger effect at bluer wavelengths, can cause a significant variation of the planetary radius was found between the \( g' \) and the \( z' \) bands. The variation is roughly 11 pressure scale height. A similar variation was found for different starspot temperatures. Such corrections are needed to accurately determine the integrated flux ratio of the WASP-36 b transmission spectrum.

To investigate this variation, we have compared the observed transmission spectrum of WASP-36 b with sets of model atmospheres. These models were calculated using 10,000 Monte Carlo simulations. We used two different codes, PETITCODE and VSTAR. These two codes produced consistent results, with a maximum difference of 0.0035 in the transmission depth for unocculted spots, which is plotted in Fig. 8, assuming a total of 1 per cent at a reference wavelength of 600 nm (Smith et al. 2011) for different starspot temperatures. Such corrections have been applied to the values of \( k \) reported in Fig. 7 for each of the four optical bands, but the difference between the blue and the red bands remains substantial.

In order to investigate this variation, we have compared the observed transmission spectrum of WASP-36 b with sets of synthetic transmission spectra. These have been obtained by using two different codes, PETITCODE and VSTAR. These two codes and the various models are described in the next two subsections.

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6 The pressure scale height is defined as \( H = \frac{k_B T_r}{\mu_{\text{mol}} g_r} \), where \( k_B \) is Boltzmann’s constant and \( \mu_{\text{mol}} \) is the mean molecular weight.
5.1 PETITCODE

For calculating synthetic transmission spectra we used PETITCODE for self-consistent modelling of one-dimensional atmospheric structures and spectra (Mollière et al. 2015). PETITCODE has recently been extended for deriving transmission spectra by directly calculating the transmission through planetary annuli as probed during transits. An effective planetary radius is then calculated from the combined transmission of all annuli. The transmission spectra include Rayleigh scattering of H₂ and He, using the cross-sections reported in Dalgarno & Williams (1962) and Chan & Dalgarno (1965), respectively. For verification purposes of our implementation of the transmission-spectrum calculations, we compared to the one-dimensional transmission spectra given in figs 2 and 3 in Fortney et al. (2010), which yielded excellent agreement. We further added molecular cross-sections for TiO and VO, using an updated line list obtained from Betrand Plez (private communication) for VO. The partition functions were obtained from Uffe Græ Jørgensen’s website7 for TiO and Betrand Plez (private communication) for VO, which is based on an updated partition function by Sauval & Tatum (1984); see also Gustafsson, Edvardsson & Eriksson (2008). As pressure broadening information was not available, we approximated the broadening coefficients using equation (15) in Sharp & Burrows (2007). For this set of models we use an extended list of condensable species, comprising MgSiO₃, Mg₂SiO₄, SiC, Fe, Al₂O₃, Na₂S, KCl, H₂O, TiO and VO. The chemical equilibrium abundances for the gas and condensed phase species in PETITCODE are now calculated by a new chemical equilibrium code, which reliably works for temperatures between 60 and 20 000 K and has been tested for consistency with the CEA code (Gordon & McBride 1994; McBride 1996). For the development of this code we made use of the methods and equations outlined in the CEA manual (McBride 1996).

Using the values reported in Table 4 for the parameters of WASP-36 b and its host star, we calculated self-consistent atmospheric structures. The stellar irradiation was calculated assuming a global average. As the flux is received by the planet with a cross-section of $\pi R_p^2$, but is distributed over an area of $4\pi R_p^2$, this corresponds to a flux dilution factor of 1/4 when compared to the flux at the sub-stellar point. We computed atmospheres for two different planetary metallicities: [Fe/H]ₚ = −0.3, which is close to the value reported for the host star (−0.26 ± 0.10, Smith et al. 2012), and [Fe/H]ₚ = 0.7, which corresponds to the planet being 10 times more enriched than its host star. For both metallicities we calculated two atmospheres: in the first case we did not consider the opacities of TiO and VO and in the atmospheric structure calculation, whereas in the second case we did consider such opacity contributions. For the cases in which TiO and VO were not considered, we took the resulting two pressure-temperature structures and calculated three different transmission spectra to investigate the following three cases:

(i) nominal case, using the same opacities as were used for obtaining the atmospheric structure;
(ii) case without Na and K opacity;
(iii) case without Na and K opacity and a H₂ Rayleigh cross-section enhanced by a factor of 1000 in order to mimic strong Rayleigh-like scatterers.

In total, we considered eight cases: 2 × 3 cases for the atmospheric structures calculated without TiO and VO, plus two cases for the atmospheric structures including TiO and VO. They are depicted in Fig. 7, and it is clear that none of the options explored above was able to reproduce the data, especially their steep slope.

The slope of the transit spectrum is given by (see, e.g. Lecavelier des Etangs et al. 2008)

$$\frac{dR_p}{d\log(\lambda)} = \alpha H$$

where $\alpha$ is the power-law dependency of the opacity with respect to wavelength, $\alpha = \frac{d\log(\kappa)}{d\log(\lambda)}$, and $H$ is the atmospheric scale height. The surface gravity of WASP-36 b is well constrained by its mass and radius measurements, and $\mu_m$ should have a value close to 2.3 au if one assumes an atmosphere dominated by H₂ and He (de Wit & Seager 2013). For WASP-36 b the slope obtained for the synthetic transmission spectra is too small by a factor of ~4 when compared to the data. The minimum temperature in our

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7 http://www.pages-perso-bertrand-plez.univ-montp2.fr/
atmospheric structure is $\sim 1000$ K. Rayleigh scattering ($\alpha = -4$) would thus require a very high atmospheric temperature, of at least 4000 K, in order to be consistent with the data.

5.2 VSTAR

We created a second set of models of the atmosphere of WASP-36 b with the Versatile Software for the Transfer of Atmospheric Radiation (VSTAR; Bailey & Kedziora-Chudczer 2012). VSTAR is a robust line-by-line radiative transfer solver, which has been successfully applied to the atmospheres of cool stars, Solar system planets, and hot Jupiters (Zhou et al. 2015). For WASP 36 b, the Rayleigh and Mie scattering capabilities were used for attempting to model the dramatic increase with radius at bluer wavelengths. Rayleigh scattering from a H–He atmosphere alone is not able to describe the change in radius for WASP 36 b that we have measured. A Mie scattering haze of small particles can be introduced to compensate for a large portion of the short wavelength absorption.

Such a scattering haze is introduced within the radiative transfer model and is dependent upon the optical depth per horizontal layer, the refractive indices of the scattering material across relevant wavelengths, and the radii of the particles themselves. Scattering atmospheric particles with radii ranging from 0.01 to 0.1 $\mu$m were tested. The distribution in sizes for a given median radius is described by a power-law distribution with an effective variance of 0.01 $\mu$m (Mishchenko, Travis & Lacis 2002). Approximately half the slope can be derived with particle sizes around 0.03 – 0.04 $\mu$m. Changing the distribution of these particles vertically throughout the atmosphere can shape the Mie scattering contribution. In systems with sufficient data, this can be fit to provide information about the cloud and haze distribution on the planet. The opaqueness of the layers set by the optical depth per height affects the spectrum particularly for upper layers where the transmission path length is longer. Too great an optical depth at a given layer will create a flattened spectrum towards longer wavelengths masking molecular features. Because of the shift in the relative radius from blue to red wavelengths for WASP 36b, it is unlikely that a very opaque cloud is present high in the atmosphere.

In Fig. 9 transmission spectral curves without molecular features are shown. The variation in the radius is due solely to scattering by molecular species or clouds and hazes. The various lines correspond to different values of the optical depth in the upper atmosphere over 1000 km. The model with H-He Rayleigh scattering alone (dashed cyan line) does not compensate for the steep rise in absorption towards blue wavelengths. The optical depth distributions shown are indicative of the effects of clouds and hazes. Blue scattering haze in a highly extended atmosphere could possibly produce the large-scale height distribution of radii.

Layer-by-layer calculations for varying optical depth were trialled, but we found that they cannot compensate for the unusually steep absorption. The scattering properties were based upon those of enstatite, which is a species likely responsible for the blue light scattering in the hot Jupiter HD 189733 b (Zahnle et al. 2009). Other species with weaker attenuation at blue wavelengths, such as some sulphurous molecular species, may better compensate for the blue light absorption in the planet’s transit. It is possible that along with strong Mie and Rayleigh scattering – perhaps from an extended scattering haze – that absorption in blue light from a molecular species is also present.
The variation between radius to that of the star in the four GROND passbands. Our data measured the orbital ephemeris and physical parameters of the system. Furthermore, the VSTAR code was also utilized to produce atmospheric structures and two opposite planetary metallicities; various opacities is therefore more likely, but the exact nature and origin of such an absorber is speculative. The existence of an absorber which reproduces the observed transmission photometry due to its line profile Alemán (CAHA) at Calar Alto, Spain. Operation of the MPG 2.2 m telescope is jointly performed by the Max Planck Gesellschaft and ESO, service operated by Cornell University.

6 CONCLUSIONS

We have presented new broad-band photometric observations of five transit events in the WASP-36 planetary system, which is composed of a relatively young G2 V star and a massive hot Jupiter. Four transits were observed with the GROND instrument, which supports observations in four optical bands simultaneously; another single-band transit observation was obtained with the CAHA 1.23 m telescope. We fitted the light curves using the JKTEBOP code, and revised the orbital ephemeris and physical parameters of the system. Our results are consistent with and more precise than previous measurements.

We searched for a variation of the measured radius of WASP-36 b as a function of wavelength by determining the ratio of the planet’s radius to that of the star in the four GROND passbands. Our data clearly show an increase of the planetary radius in the bluer bands. The variation between $g'$ and $z'$ is more than 10 $H$ with a significance level larger than $5\sigma$.

We compared the multi-band measurements with the predictions of several theoretical models of planetary atmospheres. Synthetic spectra were computed using PETITCODE for self-consistent atmospheric structures and two opposite planetary metallicities; various cases with strong absorbers (TiO and VO), without Na and K opacity and with strong Rayleigh-like scattering process, were investigated. Furthermore, the VSTAR code was also utilized to produce atmospheric models in which the planetary-radius variation is only due to scattering by molecular species or clouds and hazes. Different models were presented varying the optical depth of the atmosphere. However, in no case were our models able to reproduce the observed spectrum. Neither the presence of gaseous oxides nor strong Rayleigh scattering seems to be the cause of the steep slope in the transmission observations. The existence of an absorber which reproduces the observed transmission photometry due to its line opacities is therefore more likely, but the exact nature and origin of such an absorber is speculative.

In conclusion, the mechanism responsible for the steep slope in the transmission spectrum of WASP-36 b remains difficult to constrain. Further observations of WASP-36 b transits are suggested, especially with a photometer in the $U$ band or with a spectrograph able to cover a large spectral range at optical wavelengths.

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